

CENTER FOR TOKAMAK TRANSIENTS SIMULATION

M₃D-C₁ Code Development

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CTTS Meeting

Auburn, AL

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M3D-C1 Code Development Is Focused on Modeling Disruptions

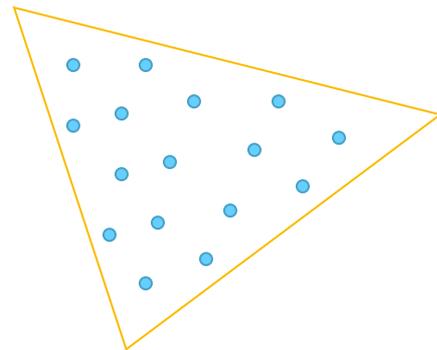
- Resistive wall model is crucial for modeling current quench and wall forces
 - Basic capability is implemented and tested
 - Future improvements will include more complicated wall
- Impurity model is necessary for modeling thermal quench
 - Now implemented in M3D-C1. Uses KPRAD to calculate ionization, recombination, and radiation
- Pellet model / coupling to FronTier
 - Parks ablation model implemented by A. Fil before impurity modeling was implemented (needs to be updated)

KPRAD Model Implemented in M₃D-C₁

- KPRAD calculates ionization, recombination, and radiation from impurities

$$\frac{\partial n_z}{\partial t} = I_{z-1} n_{z-1} - (I_z + R_z) n_z + R_{z+1} n_{z+1}$$

- All charge state densities for single impurity are evolved in time
 - Integration of master equation requires a few (variable) timesteps per MHD timestep. Done at each quadrature point independently.
 - FE representation of n_z fields calculated at each MHD timestep
 - All ionized states advected using fluid velocity
- Calculates losses from line radiation, bremsstrahlung, ionization, and recombination



Charge States and Radiation Evolve on Comparable Timescale to Disruption Dynamics

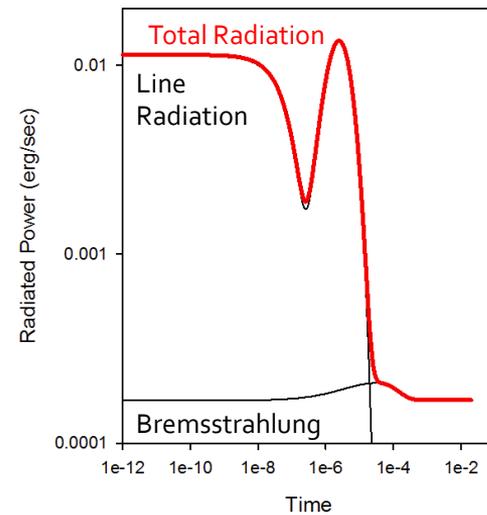
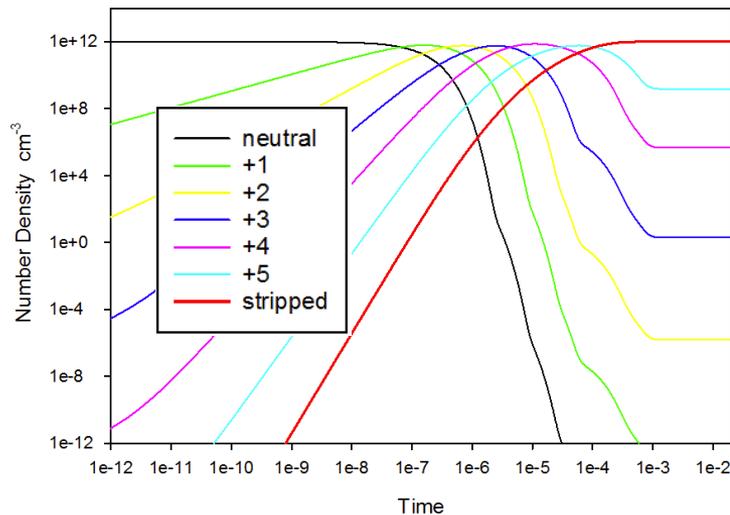
- Distribution differs significantly from steady-state distribution on timescales less than ~ 1 ms
- Need to evolve charge state densities to get accurate electron source and radiation rates during disruption

o-D test of KPRAD model with C impurity

$$n_C = 10^{12} \text{ cm}^{-3}$$

$$n_e = 10^{14} \text{ cm}^{-3}$$

$$T_e = 1 \text{ keV}$$



Single-Fluid Model with Single Impurity Species Now Implemented in M₃D-C₁

- Equations generalized to allow n_e / n_i to vary in space in time
- Single-fluid model implemented ($\mathbf{u}_e = \mathbf{u}_i = \mathbf{u}_z$)
- All ions (main & impurities) assumed to have same temperature T_i

$$\frac{\partial n_i}{\partial t} + \nabla \cdot (n_i \mathbf{u}) = \sigma_i$$

$$\rho \left(\frac{\partial \mathbf{u}}{\partial t} + \mathbf{u} \cdot \nabla \mathbf{u} \right) = \mathbf{J} \times \mathbf{B} - \nabla p - \nabla \cdot \Pi$$

$$\frac{\partial B}{\partial t} = \nabla \times (\mathbf{u} \times \mathbf{B} - \eta \mathbf{J})$$

$$\frac{\partial n_z}{\partial t} + \nabla \cdot (n_z \mathbf{u}) = \sigma_z$$

$$\rho = m_i n_i + \sum_z m_z n_z$$

$$n_e = Z_i n_i + \sum_z z n_z$$

$$\sigma_e = Z_i \sigma_i + \sum_z z \sigma_z$$

$$\mathbf{J} = \nabla \times \mathbf{B}$$

- Several models for pressure advance implemented

Collisional Terms Are Modified to Include Effects of Impurities

- Resistivity and equipartition terms include effect of electron—impurity collisions

$$\eta = \frac{m_e \nu_{eH}}{n_e e^2} \underbrace{\left(\frac{Z_i^2 n_i + \sum_z z^2 n_z}{n_e} \right)}_{Z_{\text{eff}}}$$

$$Q_\Delta = 3 \nu_{eH} \frac{m_e}{m_i} (T_i - T_e) \left(Z_i^2 n_i + \frac{m_i}{m_z} \sum_z z^2 n_z \right)$$

$$\nu_{eH} = \frac{4\sqrt{2}\pi e^4 n_e \ln \Lambda}{3\sqrt{m_e T_e^{3/2}}} \quad \text{electron-ion collision frequency if plasma were purely hydrogenic}$$

- Other collisional terms (viscosity, thermal diffusivity) are anomalous and are not modified by impurities (presently)

Four Models for Pressure Advance Implemented

1. Single equation for total pressure. Assumes $p_e / p = \text{const.}$

$$\frac{\partial p}{\partial t} + \mathbf{u} \cdot \nabla p + \Gamma p \nabla \cdot \mathbf{u} = (\Gamma - 1)(Q + \nabla \cdot \mathbf{q} + \Pi : \nabla \mathbf{u} + \eta J^2)$$

2. Single equation for temperature (from sum of all temp. equations).
Assumes $T_e / T_i = \alpha$.

$$N \left(\frac{\partial T_e}{\partial t} + \mathbf{u} \cdot \nabla T_e + (\Gamma - 1) T_e \nabla \cdot \mathbf{u} \right) + \Sigma T_e = (\Gamma - 1)(Q + Q_{rad} + \nabla \cdot \mathbf{q} + \eta J^2 + \Pi : \nabla \mathbf{u})$$

$$N = n_e + \alpha \left(n_i + \sum_z n_z \right)$$

$$\Sigma = \sigma_e + \alpha \left(\sigma_i + \sum_z \sigma_z \right)$$

3. Two pressure equations: one for total pressure, one for electron pressure

$$\frac{\partial p_e}{\partial t} + \mathbf{u} \cdot \nabla p_e + \Gamma p_e \nabla \cdot \mathbf{u} = (\Gamma - 1)(Q_e + Q_{rad} + Q_{\Delta} + \nabla \cdot \mathbf{q}_e + \eta J^2)$$

4. Two temperature equations: one for electron temperature, one for ion temperature (sum of all ion temp. equations).

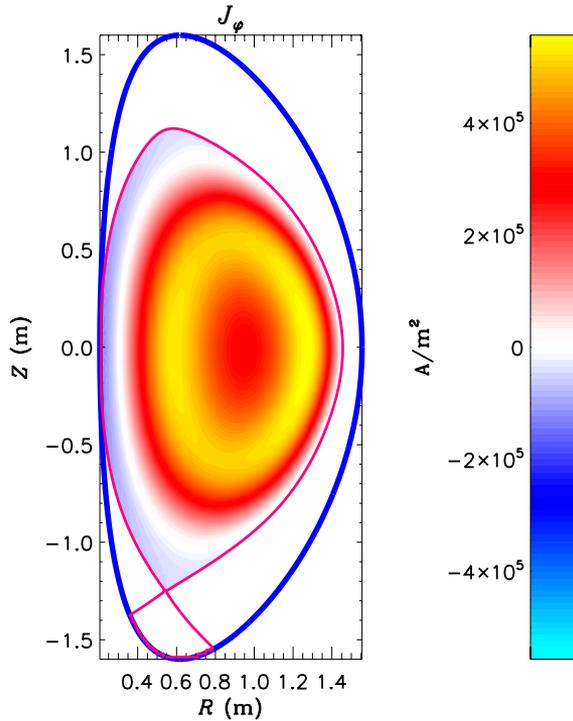
$$n_e \left(\frac{\partial T_e}{\partial t} + \mathbf{u} \cdot \nabla T_e + (\Gamma - 1) T_e \nabla \cdot \mathbf{u} \right) + \sigma_e T_e = (\Gamma - 1)(Q_e + Q_{rad} + Q_{\Delta} + \nabla \cdot \mathbf{q}_e + \eta J^2)$$

$$n_i \left(\frac{\partial T_i}{\partial t} + \mathbf{u} \cdot \nabla T_i + (\Gamma - 1) T_i \nabla \cdot \mathbf{u} \right) + \sigma_i T_i = (\Gamma - 1)(Q_i - Q_{\Delta} + \nabla \cdot \mathbf{q}_i + \Pi_i : \nabla \mathbf{u})$$

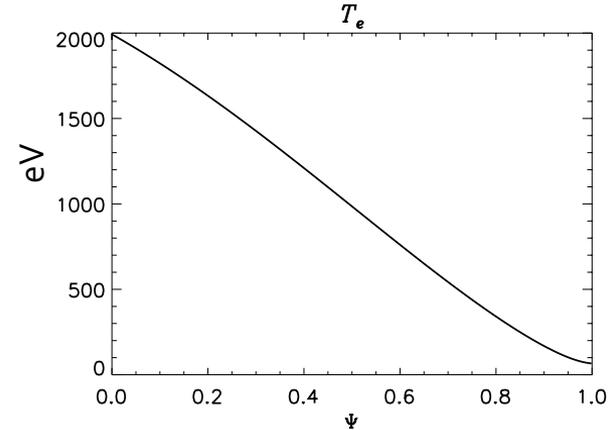
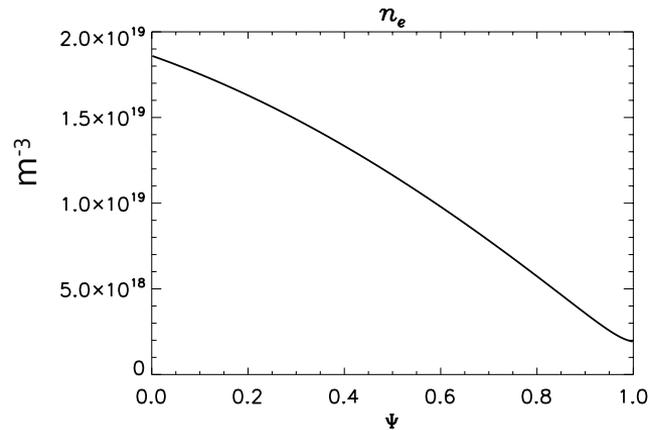
$$n_i = n_i + \sum_z n_z$$

$$\sigma_i = \sigma_i + \sum_z \sigma_z$$

Simple Test Case: Lots of Neutral Argon Introduced Globally

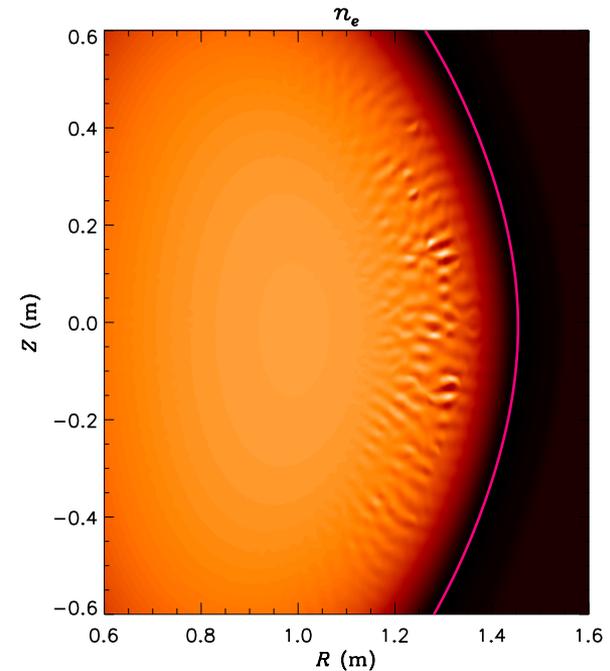


- Equilibrium is reconstruction of NSTX discharge 139536 at $t=309$ ms
- Neutral Argon is introduced globally at $n_{\text{Ar}} = 0.1\% n_{\text{D}}$.
- Initial cooling is mainly due to dilution



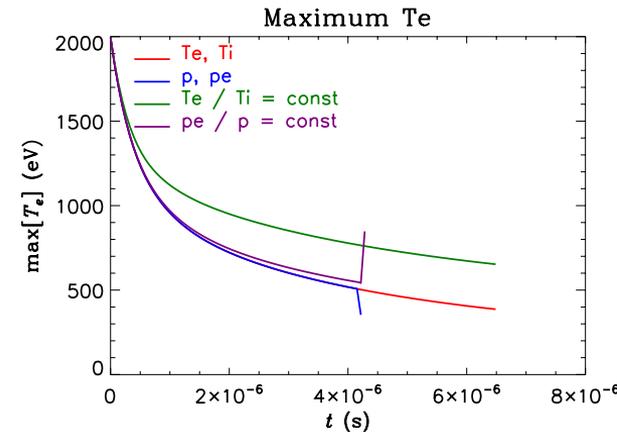
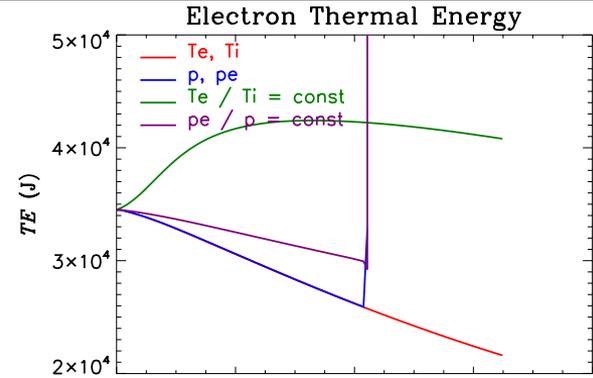
Split Pressure Advance is Numerically Unstable

- In “split” advance, \mathbf{u} , n , p (or T), and \mathbf{B} are advanced separately (in that order)
 - \mathbf{u} advance includes semi-implicit operator
- Split methods advancing p exhibit numerical instability
- “Unsplit” (Crank-Nicolson) pressure advance remains stable
 - Density, pressure, and magnetic field advanced together



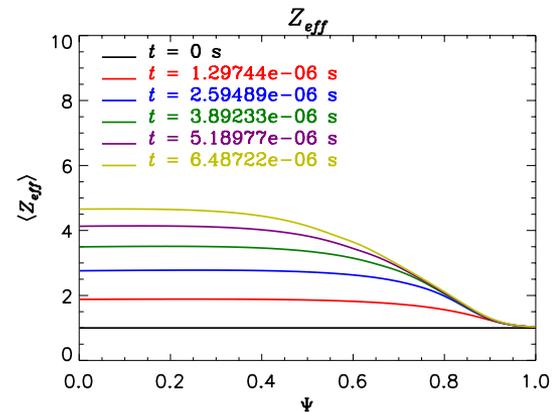
$T_e / T_i = \text{const}$ is a Bad Assumption

- Cooling mechanisms primarily affect electrons
 - Dilution from impurity electrons
 - Radiation
- This leads to T_e dropping much faster than T_i
 - $T_e / T_i = \text{const}$ is bad assumption!
- Due to significant heat fluxes during disruptions, electrons and ions probably never reach equipartition
- When cooling is dominantly due to dilution, $p_e / p = \text{const}$ is a much better assumption
 - Dilution does not remove thermal energy

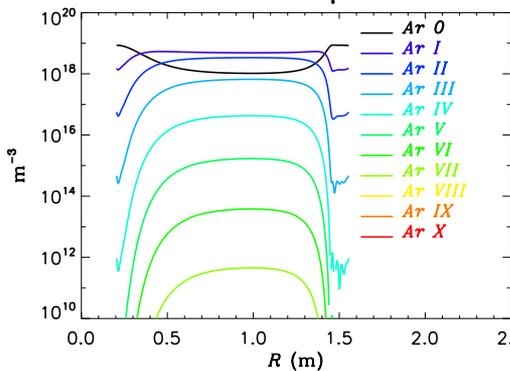


Edge Reaches Charge State Equilibrium Before Core

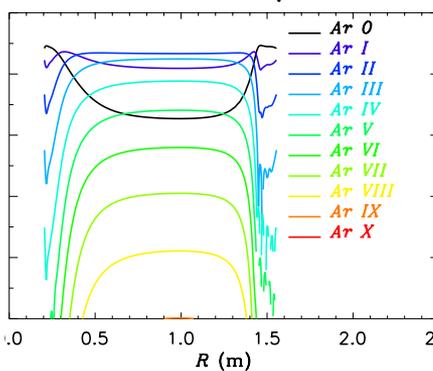
- Charge state densities in edge reach equilibrium before those in core
- Highly ionized states take $\sim 100 \mu\text{s}$ to reach appreciable levels



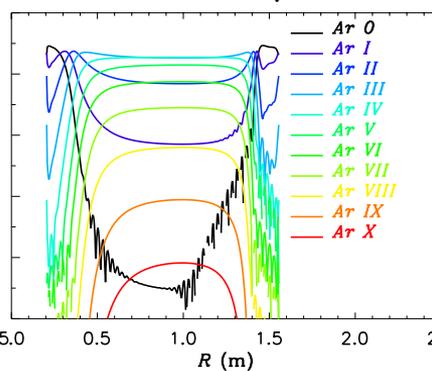
$t \sim 1.3 \mu\text{s}$



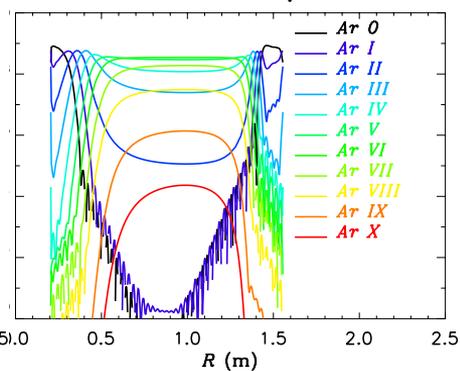
$t \sim 2.6 \mu\text{s}$



$t \sim 4.9 \mu\text{s}$



$t \sim 6.5 \mu\text{s}$



Summary and Future Plans

- Detailed impurity model is now implemented in M₃D-C₁
 - Tracks all charge states of a single impurity species
 - Uses KPRAD for ionization, recombination, and radiation
 - Uses single-fluid velocity to advect impurities
 - Benchmarking is underway (Brendan's talk)
- Future plans:
 - Non-axisymmetric / non-contiguous conducting wall structures
 - More sophisticated impurity source models (e.g. FronTier)

Non-Axisymmetric / Non-Contiguous Wall Structures in M₃D-C₁

- “Resistive Wall” region in M₃D-C₁ is a logical region of the mesh
 - Must be axisymmetric and contiguous due
- Resistivity in this region does not have to be axisymmetric or contiguous
 - Conducting structures of arbitrary complexity can be modeled in this region
 - Only restriction is that plasma can’t enter this region
- Simple rectangular “wall breaks” have already been implemented as a test of this concept

